

# Inventory Modelling Using SimPy

By Jimmy McLaughlin, Mengzhe Zhang, and Professor Anh Ninh

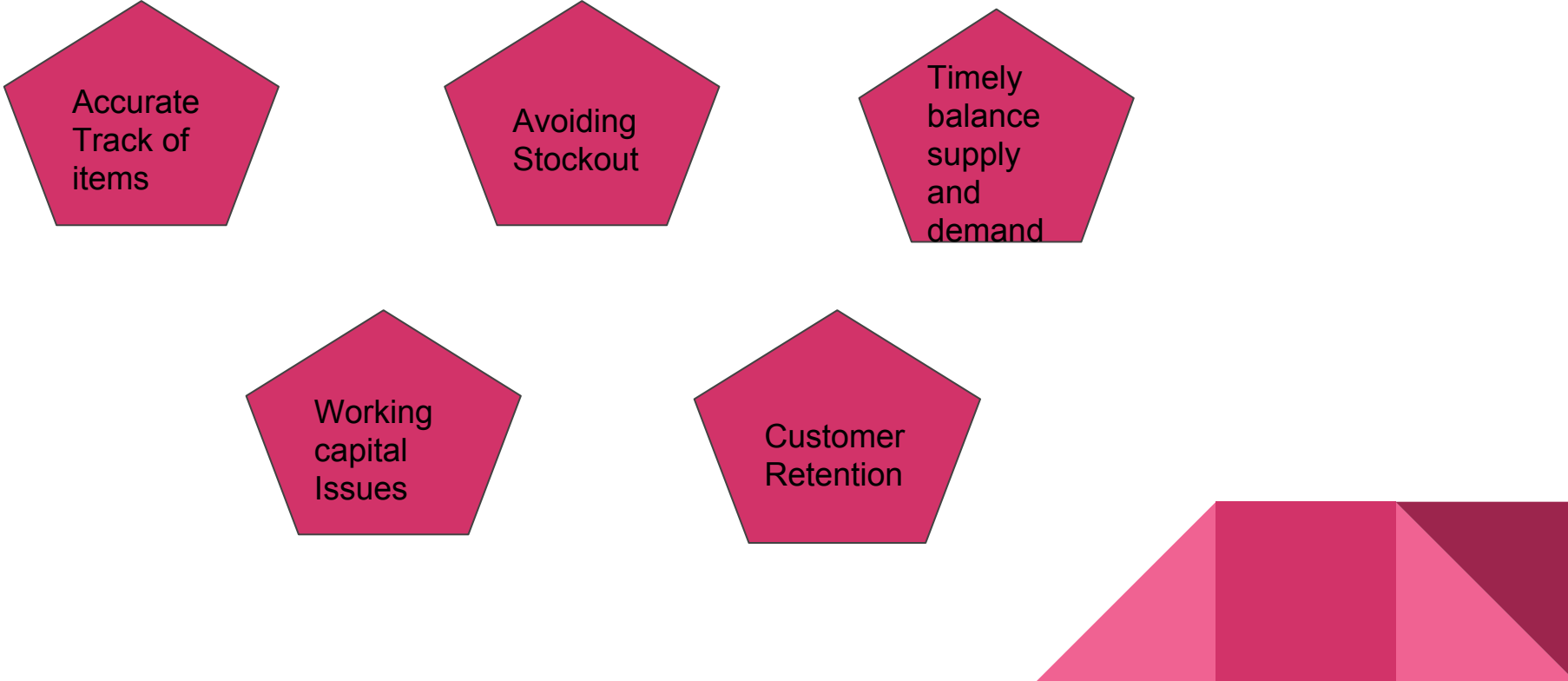


# Outline

- Overview of inventory management
- Research goal
- Modelling
  - Trade offs
  - Poisson process
  - Inventory policy
- Simulation in SimPy
- Results



# Importance of inventory management



Accurate  
Track of  
items

Avoiding  
Stockout

Timely  
balance  
supply  
and  
demand

Working  
capital  
Issues

Customer  
Retention

# Inventory management in practice

- Most widely used---spreadsheets, Access, SAP one, Syspro
- Bar codes and scanners- Universal Product Code (UPC) and personal computers made this possible for groceries



# Entities that use inventory management

Goods Based  
Companies:  
Apple, Nike,  
Gopro

Service Based  
Companies: JP  
Morgan,  
Deutsche Bank

E-Commerce  
Companies:  
Amazon,  
Alibaba

Retailers:  
Walmart,  
Costco

Manufacturer:  
Foxconn,  
Pegatron





# Research goal

Find the most efficient way to manage inventory in a simplified supply chain network with only a single store **over a given time period**

How to characterize random demand?

What is the best inventory policy?

What are the decision making criteria?





# Trade-offs in inventory management

Type of Cost

Shipping

Holding

Backorder

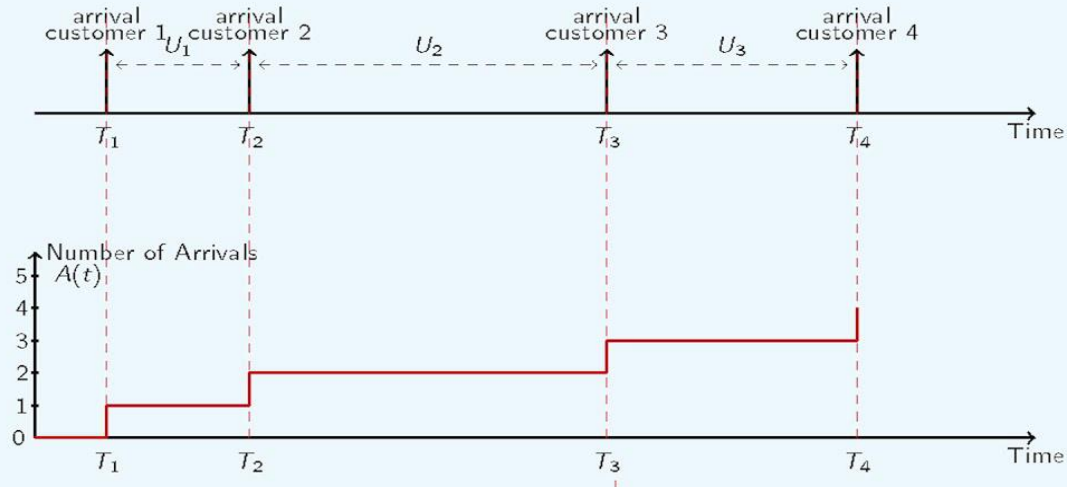
Goal

Find the optimal policy to minimize three costs combined



# Customer arrivals: Poisson process

## Characterizing Arrivals with the Counting Process



# Customer arrivals: Poisson process


- Given an arrival rate  $r$ , the probability of having  $k$  events in an interval  $t$  is given by:

$$P(k \text{ events in interval } t) = e^{-rt} \frac{(rt)^k}{k!}$$

- The inter-arrival times follow an exponential distribution with mean  $1/r$



# Inventory policy



Constant delivery  
policy

order the same number of units every day regardless of current inventory level



Order up to policy

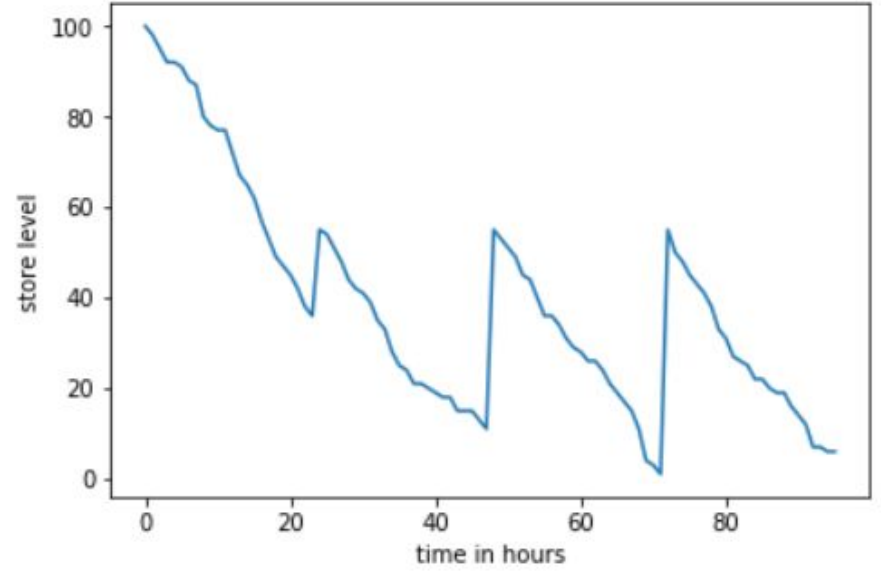
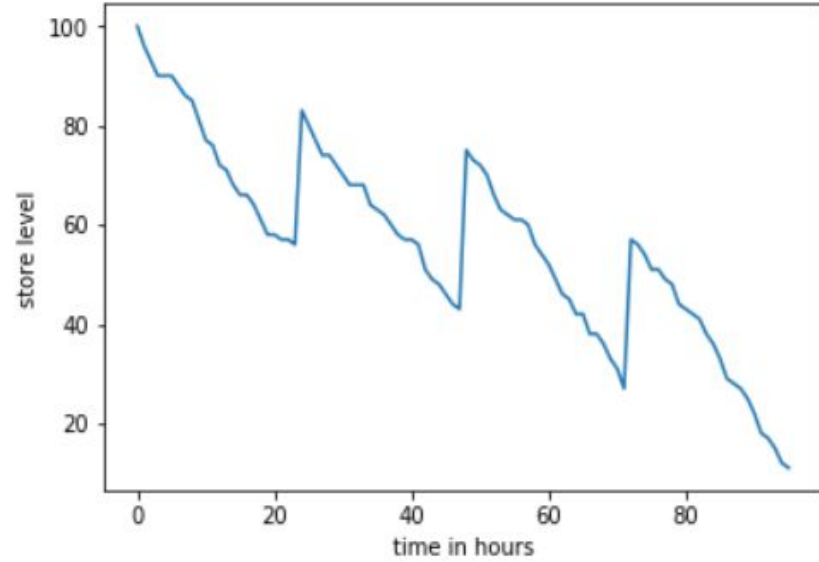
order just enough so that we start every day with the same amount of items



# Policy 1

Versus

# Policy 2



# Research questions: recap

- Which ordering policy is more cost efficient?
- If policy 1 is better, what is the ideal delivery amount?
- If policy 2 is better, what is the ideal order-up-to amount?



# Brief introduction of SimPy

- “SimPy is a process-based discrete-event simulation framework based on standard Python” -from SimPy website
- Useful for models where we want to keep track of time
- Yielding an event causes the process to get suspended, and the process will resume once the event occurs.
- SimPy is relatively new; its first release was in 2002 and the current version was released in 2016.



# Simple example

```
def car(env):  
    while True:  
        print('Start parking at %d' % env.now)  
        parking_duration = 5  
        yield env.timeout(parking_duration)  
  
        print('Start driving at %d' % env.now)  
        trip_duration = 2  
        yield env.timeout(trip_duration)
```

-from the SimPy website





# Car generator output

Start parking at 0

Start driving at 5

Start parking at 7

Start driving at 12

Start parking at 14



# Applying SimPy to our problem

- For our example, we kept the three costs constant
- Holding cost=\$8 per item
- Shipping cost= \$50+\$20 per item
- Backorder cost=\$92 per customer




# Applying SimPy to our problem


- Model customer arrival using Poisson process ( $r=2/\text{hr}$ )
- Every customer takes one item and leaves
- Customer arrival is stationary



# Applying SimPy to our problem

- Inventory is reviewed periodically every day
  - The simulation runs for 4 days
  - Keep track of items in storage, number of deliveries, number of customers that have arrived
  - Compute cost at the end of the simulation using the values of our parameters
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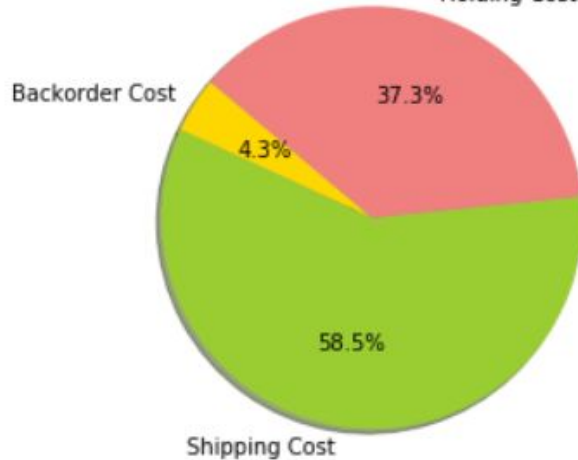
# Conclusion

- Strategy 2, the order-up-to policy is the better ordering policy
  - The ideal order-up-to amount is 55 items
  - The optimal cost for order-up-to 55 items is \$3573.929, which is broken down as follows:
    - Backlog cost: \$152.8764
    - Shipping cost: \$2089.342
    - Holding cost: \$1331.71
  - For strategy 1, the ideal delivery amount is 32 items per day
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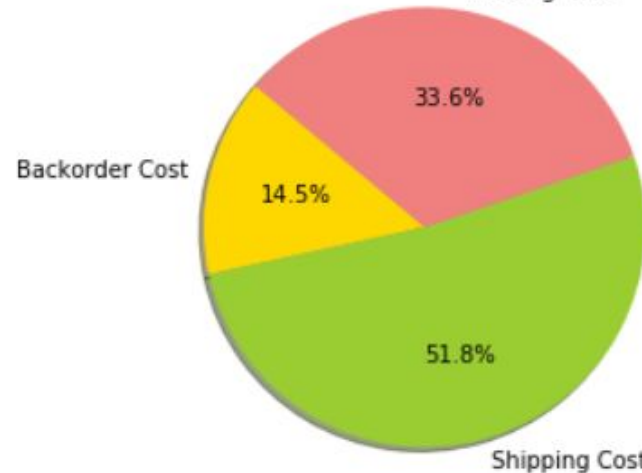
# Conclusion

- Trends in changes to backorder cost:
  - If backorder cost decreases, optimal order-up-to amount decreases
  - If we cut backorder cost in half, optimal order-up-to amount becomes 45 items

Expected Cost Distribution with backorder cost of \$92  
Holding Cost



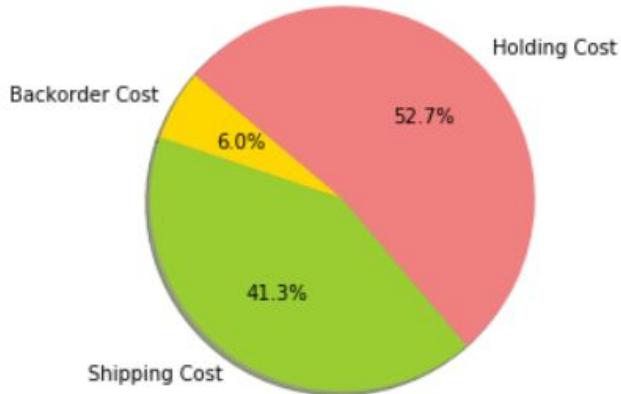
Expected Cost Distribution with backorder cost of \$46  
Holding Cost



# Conclusion

- Trends in change to shipping and holding cost:
  - If we decrease shipping and holding cost, optimal order-up-to amount increases, but not by much unless we increase both
  - In our example, cutting either shipping or holding in half does not change the delivery threshold

Expected Cost Distribution with shipping cost of \$25/10



Expected Cost Distribution with holding cost of \$4



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